

**Victoria Yankelevich**

# **Cosmology with the Euclid galaxy bispectrum**

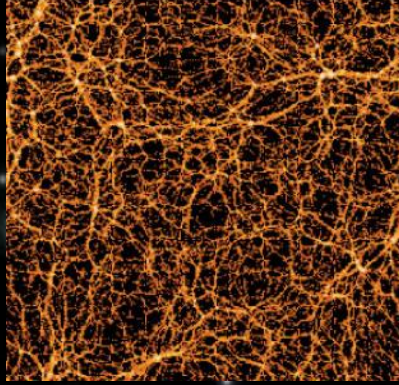
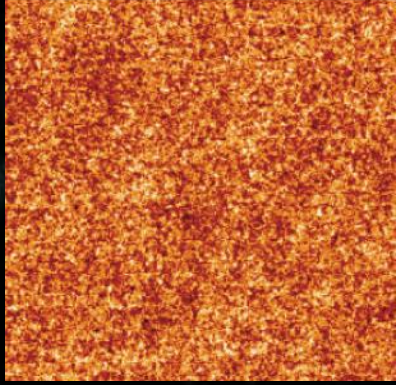
**with Cristiano Porciani**

**Argelander Institute for Astronomy, University of Bonn**

**COSMO17, Paris, August 28th – September 1st, 2017**

# Outline

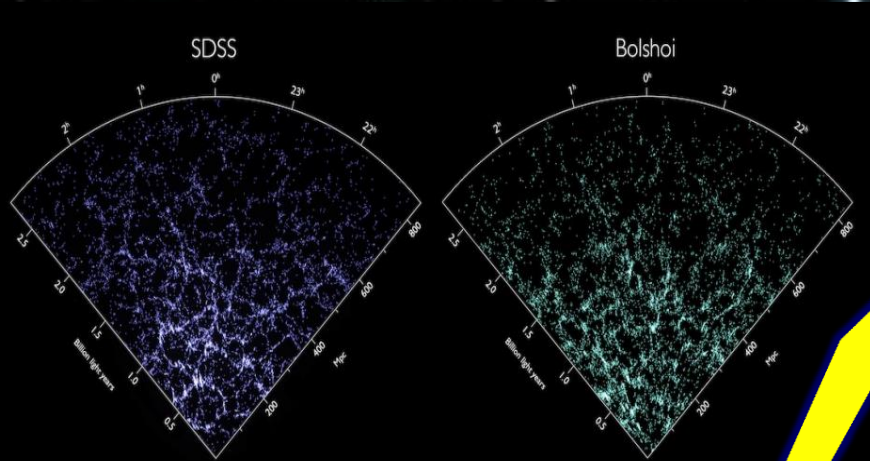
- Introduction
- Aim of the work
- Power Spectrum and Bispectrum
- Fisher-matrix formalism and Covariance matrix
- Results
- Conclusions



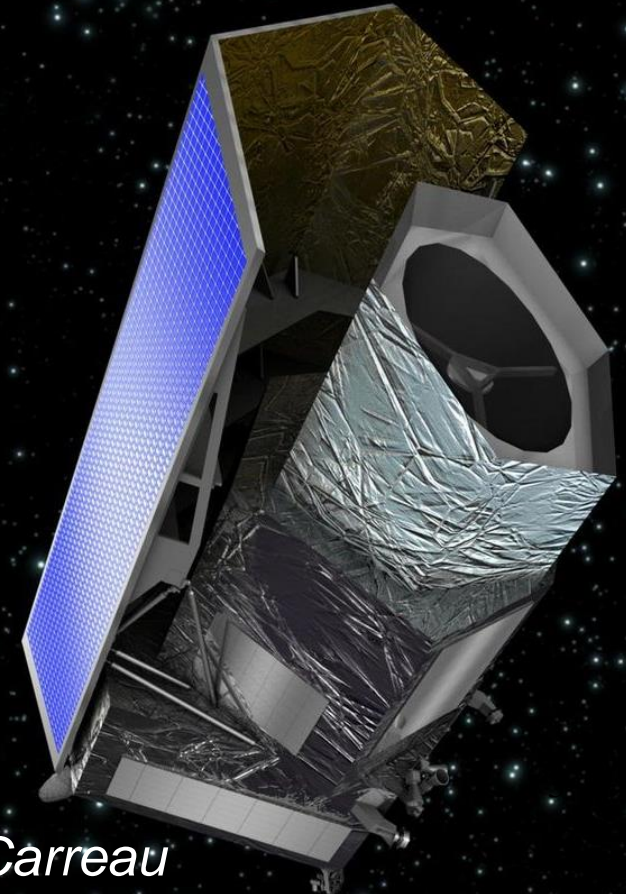
$$B(k_1, k_2, k_3) = 0 \quad B(k_1, k_2, k_3) \neq 0$$

# ESA's Euclid mission

WP  
Higher-Order statistics



Galaxy bias



# Aim of the work

## Make forecasts for the cosmological parameters for Euclid data

$\Lambda$ CDM model:  $\Omega_m, \Omega_b, n, h, A, \sigma_p, b_1, b_2, b_{s^2}$

wCDM model:  $w, \Omega_m, \Omega_b, n, h, A, \sigma_p, b_1, b_2, b_{s^2}$

$w_0 w_a$ CDM model:  $w_0, w_a, \Omega_m, \Omega_b, n, h, A, \sigma_p, b_1, b_2, b_{s^2}$

Perturbation theory (leading order)

Advantages of the combination of the power spectrum and the bispectrum in comparison with a single probe

# Power Spectrum

$$P(\mathbf{k}, \mu) = Z_1^2(\mathbf{k}, \mu) P_0(\mathbf{k}) e^{-(k\mu\sigma_p)^2},$$

$$Z_1(\mathbf{k}, \mu) = b_1 + f\mu^2, \quad \mu = \frac{k_z}{k}$$

## Bispectrum

$$B(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3, \mu_1, \varphi) =$$

$$2 \left[ Z_2(\mathbf{k}_1, \mathbf{k}_2) Z_1(\mathbf{k}_1, \mu_1) Z_1(\mathbf{k}_2, \mu_2) P(k_1) P(k_2) + \text{cyc} \right] \cdot$$

$$\cdot \exp \left[ - (k_1^2 \mu_1^2 + k_2^2 \mu_2^2 + k_3^2 \mu_3^2) \sigma_p^2 \right]$$

Galaxy bias parameters:

$b_1$  – linear,  $b_2$  non – linear,  $b_{s_2}$  – tidal bias

# Fisher Matrix

$$F_{\alpha\beta} = \sum_{\mathbf{k}}^{k_{\max}} \sum_{\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3}^{k_{\max}} \frac{\partial^t \mathbf{S}}{\partial \mathbf{x}_\alpha} \mathbf{C}^{-1} \frac{\partial \mathbf{S}}{\partial \mathbf{x}_\beta} \quad \mathbf{S} = \begin{pmatrix} \mathbf{P}(\mathbf{k}) \\ \mathbf{B}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \end{pmatrix}$$

$$\alpha, \beta : \Omega_m, \Omega_b, n, h, A, \sigma_p, b_1, b_2, b_{s_2}, w, w_0, w_a, f$$

$$\mathbf{C}_{PP}$$

$$\mathbf{C}_{BB}$$

$$\mathbf{C}(\text{diag}) = \begin{pmatrix} \mathbf{C}_{PP} & 0 \\ 0 & \mathbf{C}_{BB} \end{pmatrix}$$

$$\mathbf{C} = \begin{pmatrix} \mathbf{C}_{PP} & \mathbf{C}_{PB} \\ \mathbf{C}_{BP} & \mathbf{C}_{BB} \end{pmatrix}$$

# Covariance matrix

$$C_{PP} = \frac{4\pi}{V_s k^2 \Delta k \Delta \mu} \tilde{P}^2(k) \quad \tilde{P}(k) = \left[ Z_1^2(k, \mu) P(k) + n_g^{-1} \right]$$

$$C_{BB} = S_B \frac{8\pi^4}{V_s k_1 k_2 k_3 (\Delta k)^3 \Delta \mu \Delta \varphi} \tilde{P}_1(k) \tilde{P}_2(k) \tilde{P}_3(k)$$

$$C_{PB} = S_{PB} \frac{4\pi}{V_s k^2 \Delta k \Delta \mu} \tilde{P}(k) \tilde{B}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3, \mu_1, \varphi)$$

$$\tilde{B} = B + \left[ P(k_1) + P(k_2) + P(k_3) \right] / n_g + n_g^{-2}$$

# Results:

$$\mathbf{k}_{\max} = 0.15 \text{ hMpc}^{-1}$$

$$k_F = \frac{2\pi}{\sqrt[3]{V_s}}$$

$$\Delta k = k_F$$

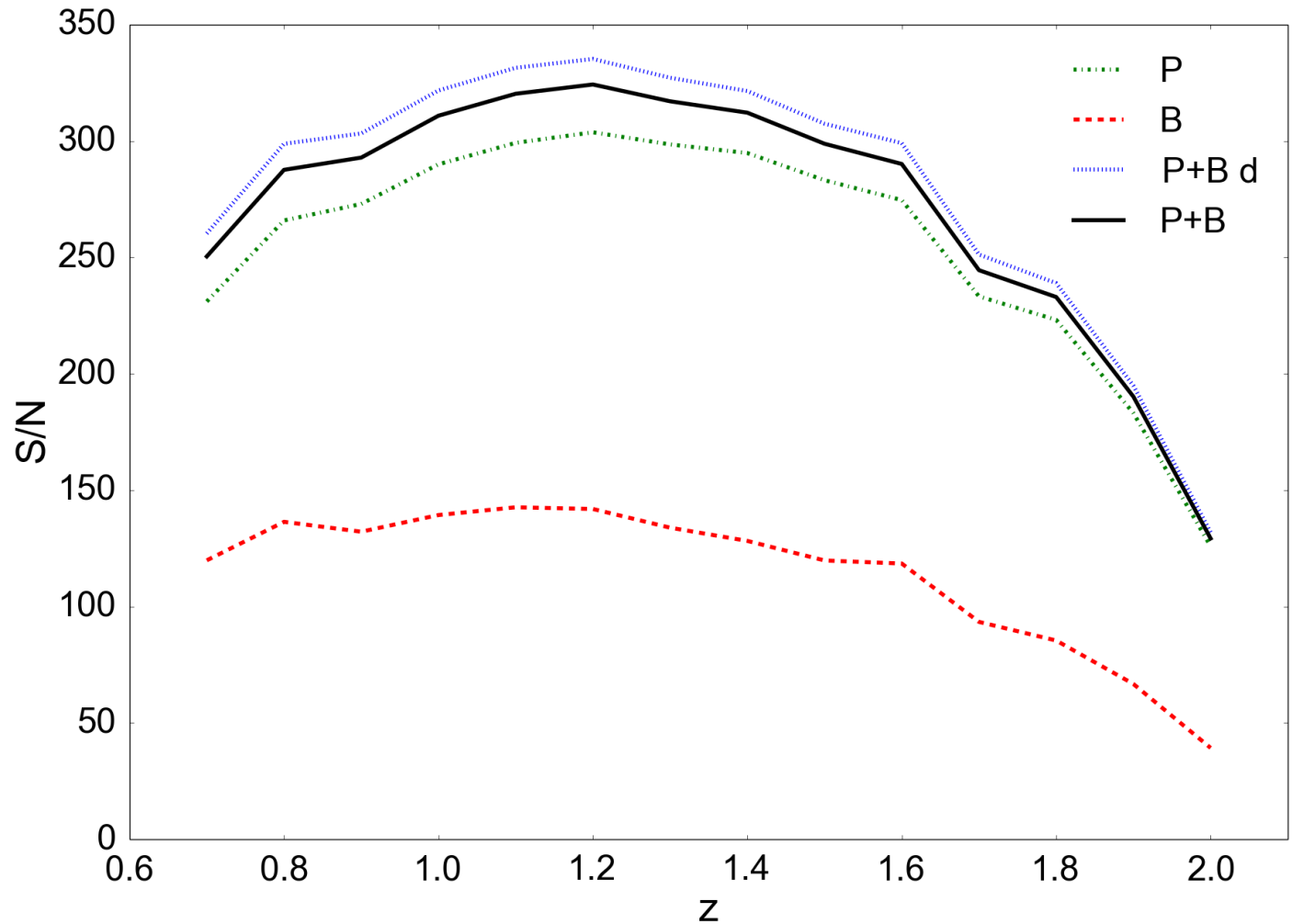
$$\Delta\mu = 0.5,$$

$$\mu \in [-1, 1]$$

$$\Delta\varphi = \pi/4,$$

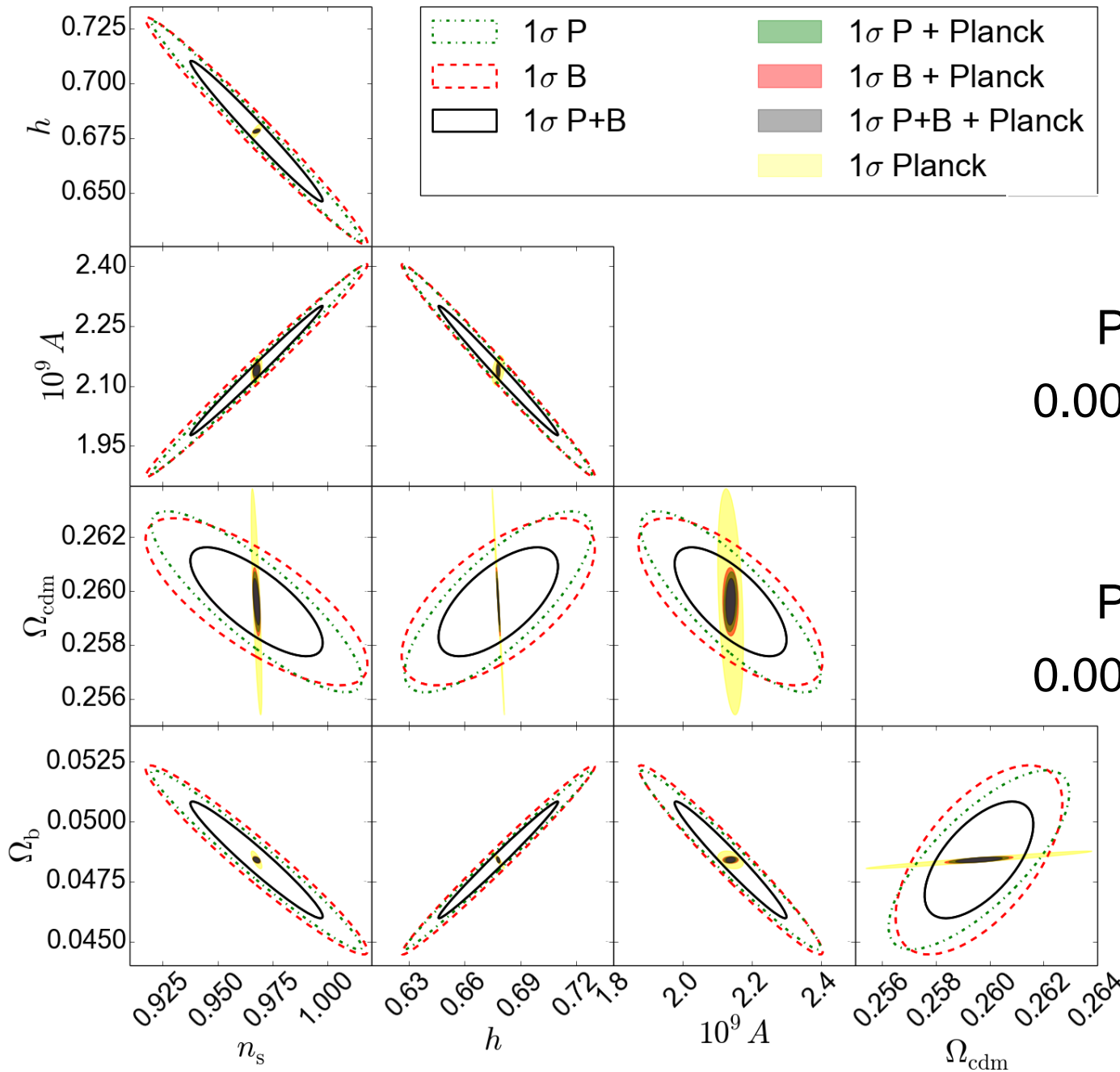
$$\varphi \in \left[-\pi/2, \pi/2\right]$$

## Signal-to-Noise





# $\Lambda$ CDM model



$1\sigma(\Omega_{\text{cdm}})$

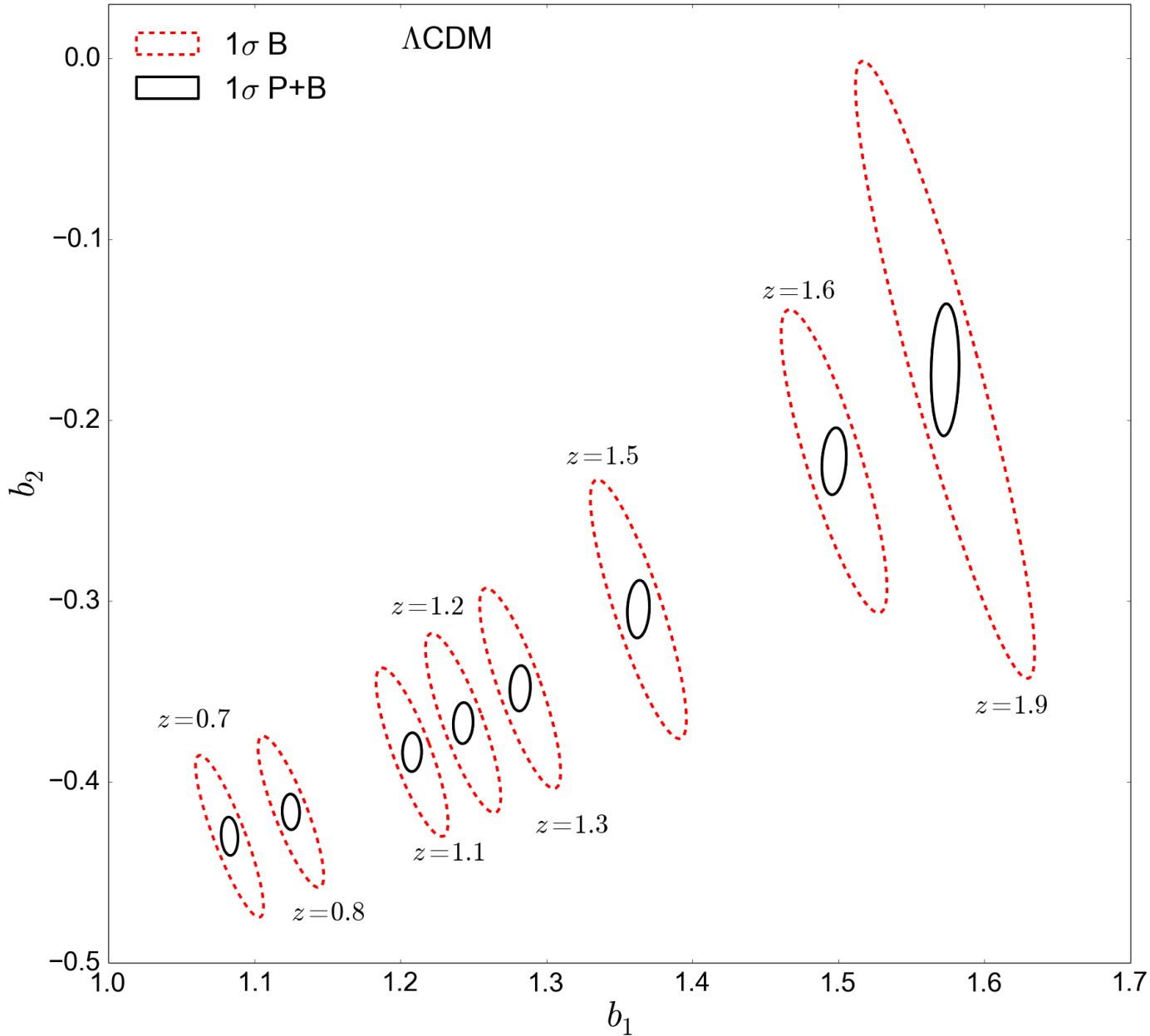
**Euclid**

	P	B	P + B
$1\sigma$ width	0.0067	0.0062	0.0040

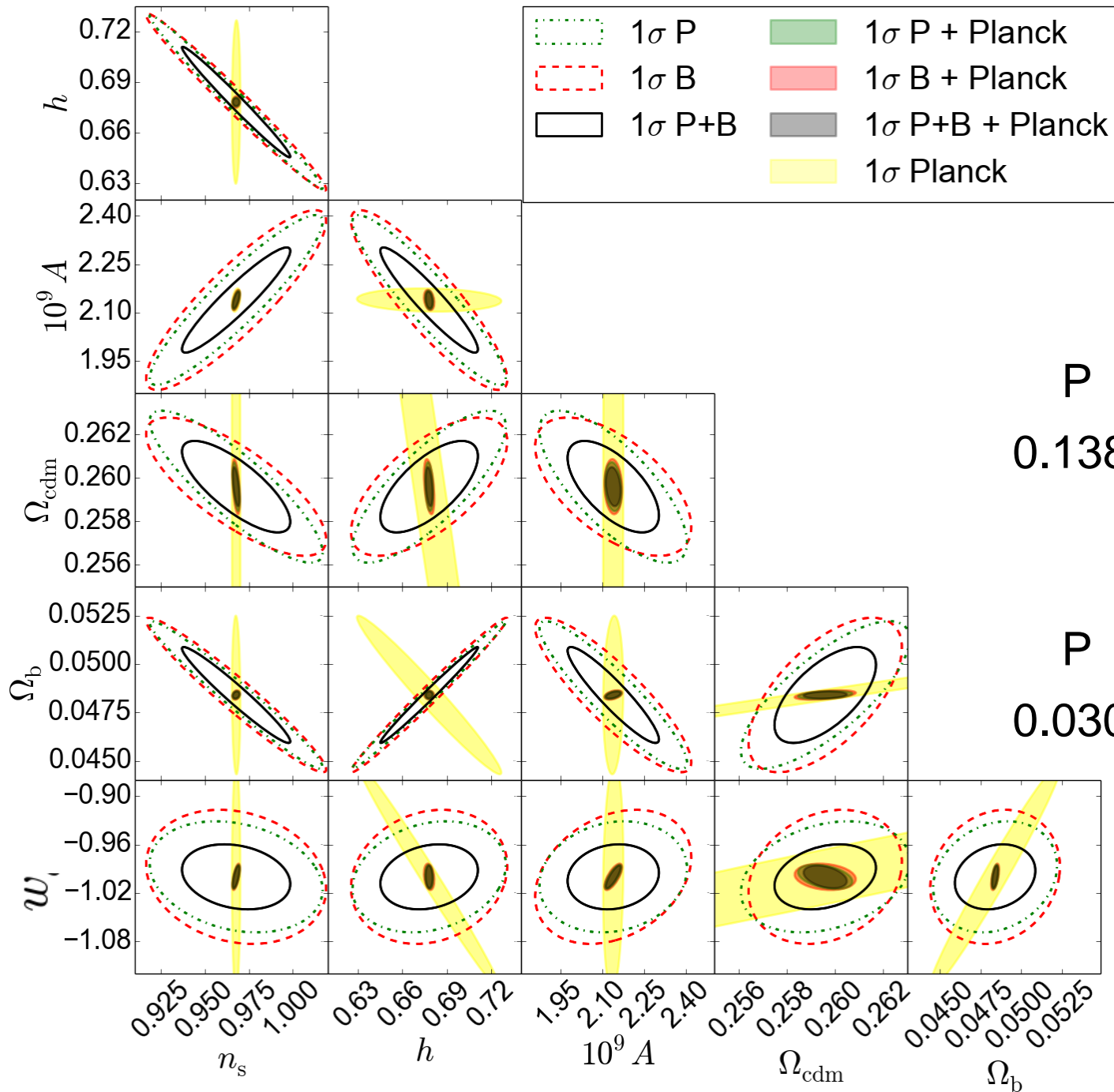
**Euclid + Planck**

	P	B	P + B
$1\sigma$ width	0.0022	0.0025	0.0017

# $\Lambda$ CDM model $\Delta b_1 \Delta b_2$



# wCDM model



1 $\sigma$ (w)

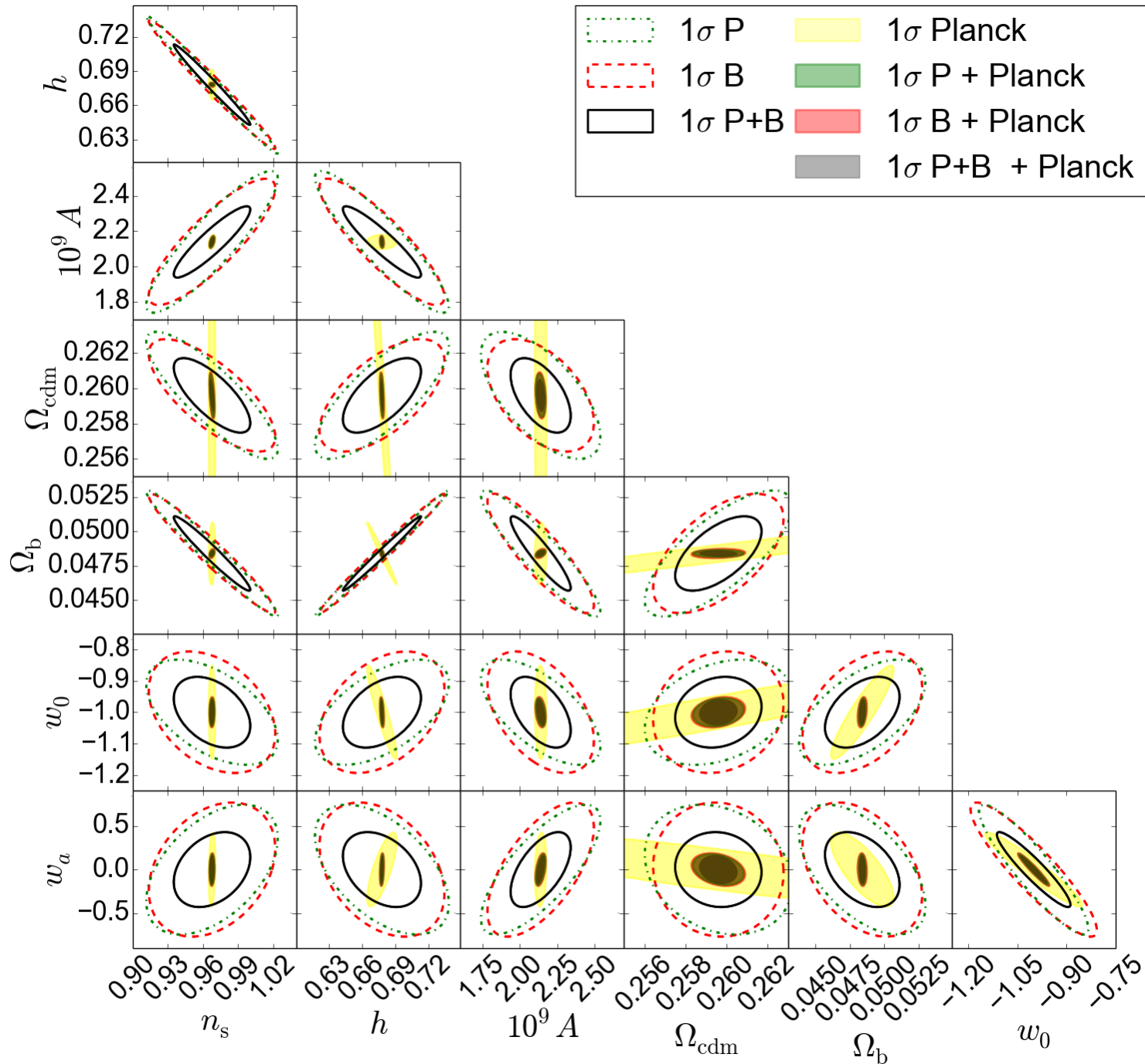
**Euclid**

	P	B	P + B
$\Omega_{\text{cdm}}$	0.138	0.166	0.081

**Euclid + Planck**

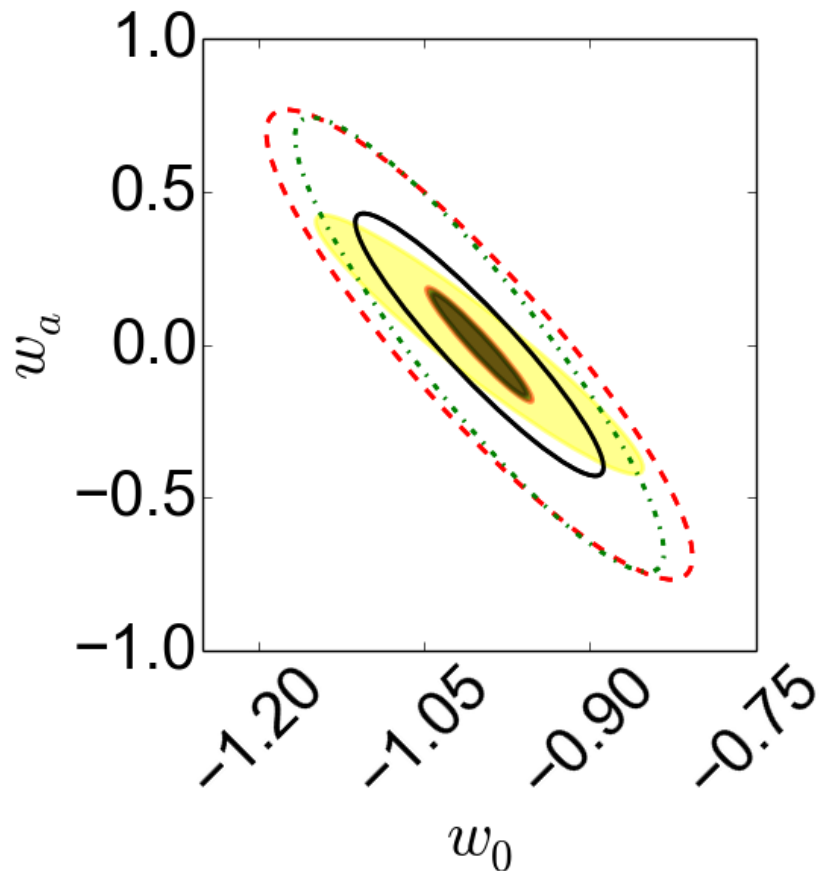
	P	B	P + B
$\Omega_{\text{b}}$	0.030	0.033	0.028

# $w_0 w_a$ CDM model

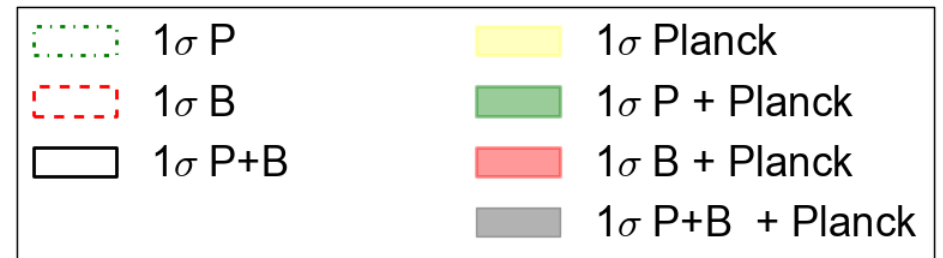


# $w_0 w_a$ CDM model

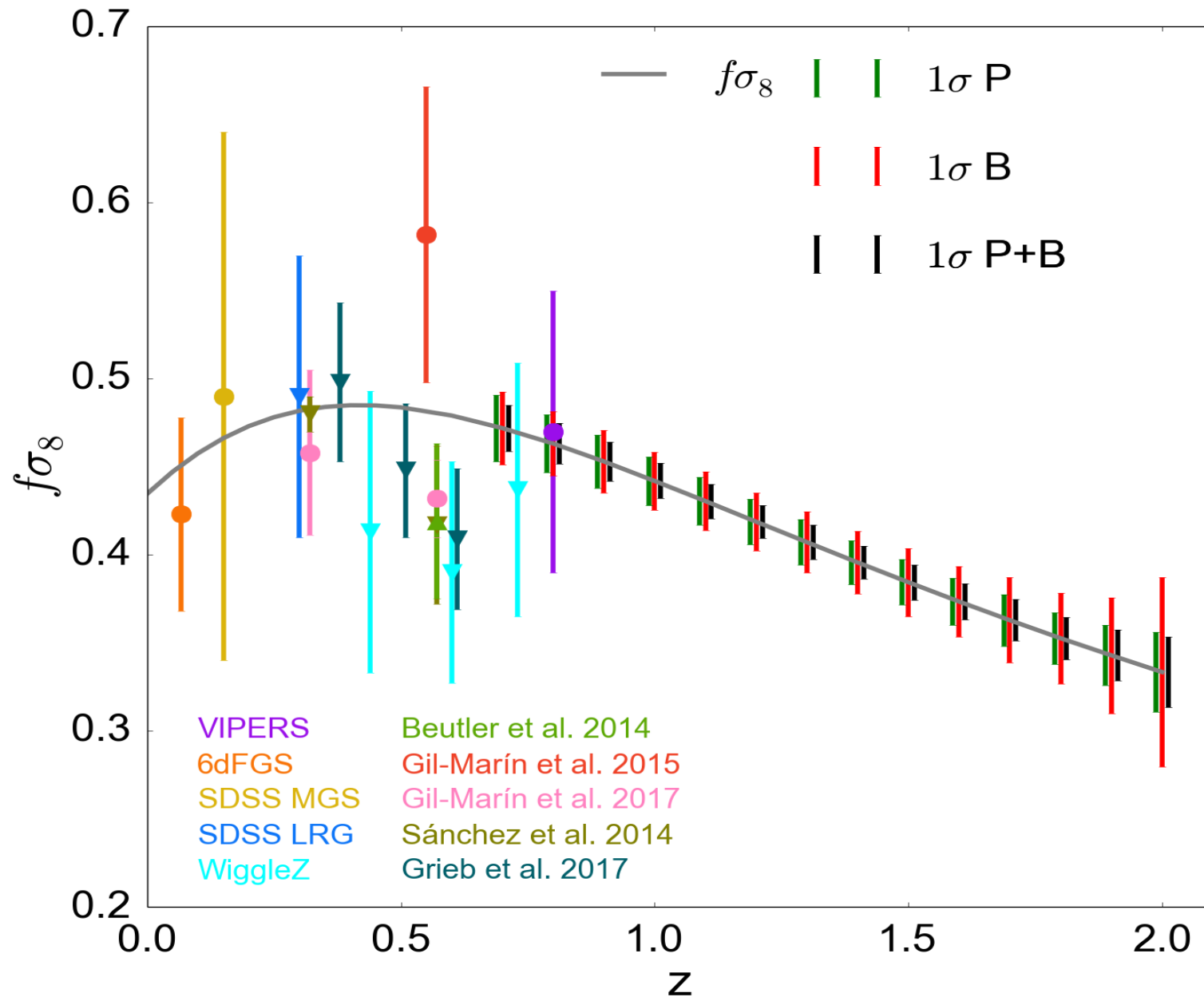
	<b>P</b>	<b>B</b>	<b>P + B</b>	<b>P + Planck</b>	<b>B + Planck</b>	<b>P+B + Planck</b>
FoM	0.58	0.47	1.72	14.61	11.75	17.55



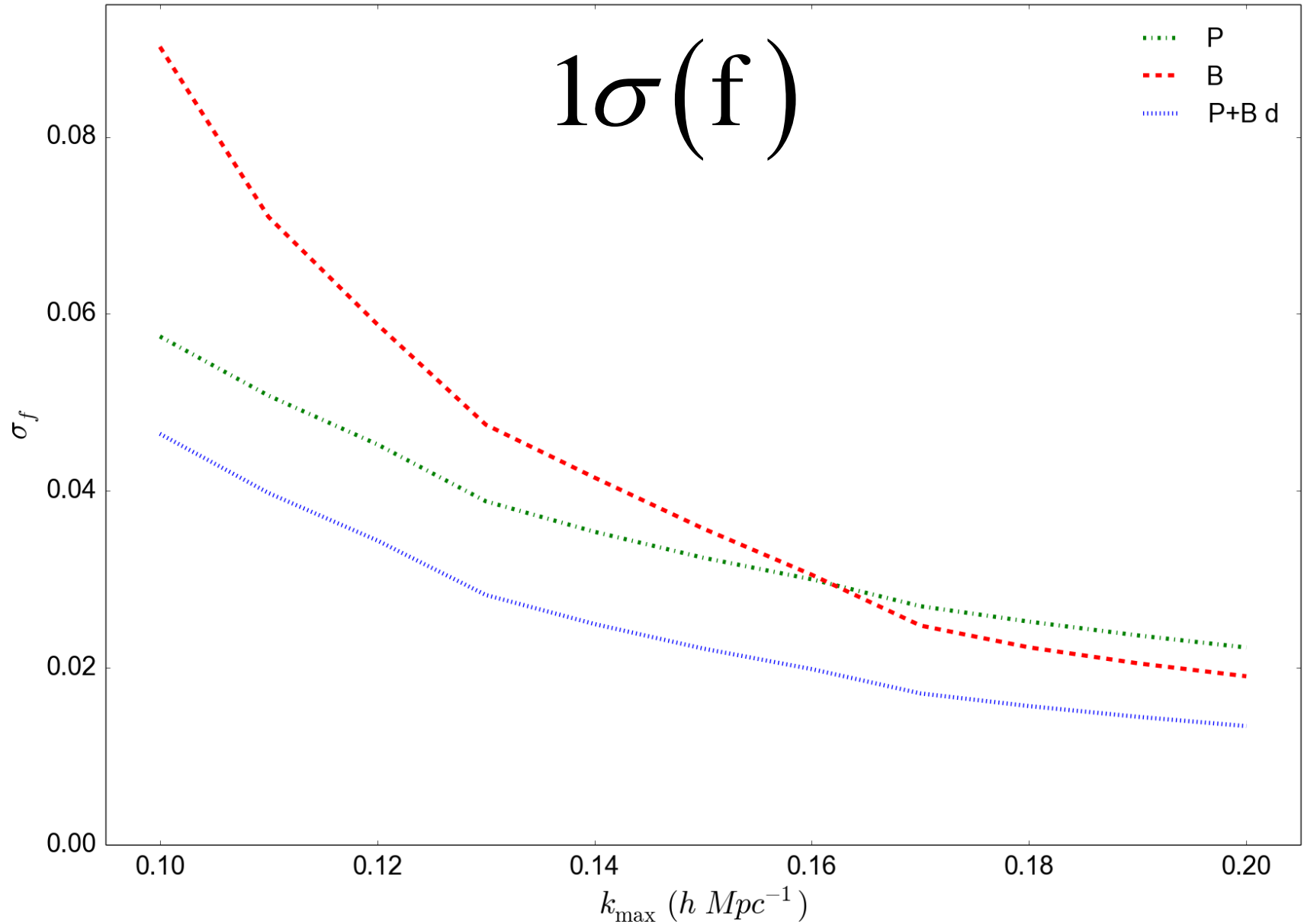
$$\text{FoM} = \frac{1}{6.17\pi\sqrt{\det(\text{Cov}(w_0 w_a))}}$$



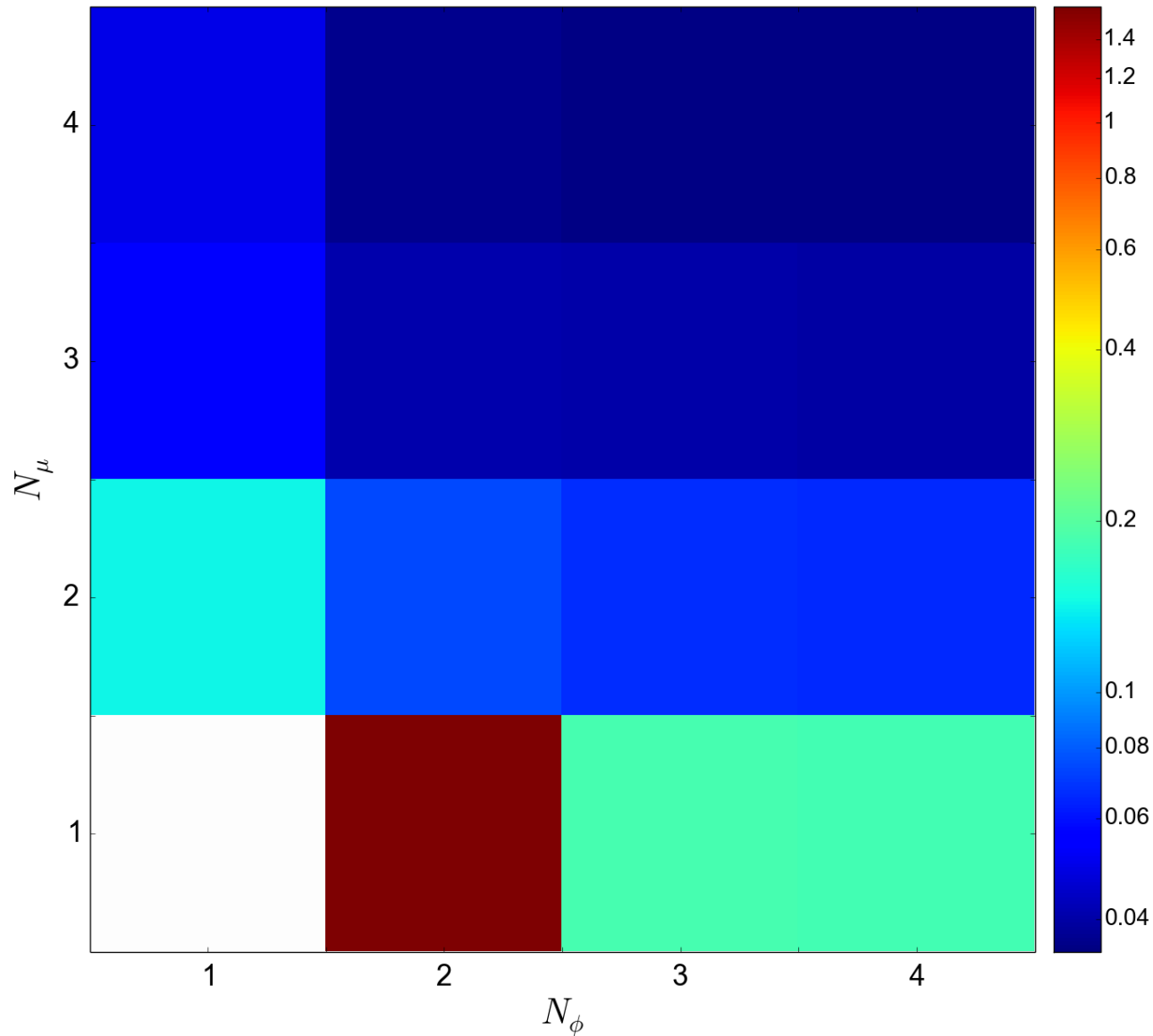
# $\Lambda$ CDM *fixed cosmology*



# Dependence on $k_{\max}$



# Dependence on $N_\mu$ , $N_\phi : 1\sigma(f)$





# Conclusions

Euclid forecast (including Planck):

$\Lambda$ CDM, wCDM,  $w_0 w_a$  CDM models

+

Galaxy bias  $b_1, b_2, b_{s^2}$

Fixed cosmology model:  $f, \sigma_p, b_1, b_2, b_{s^2}$

Combination of the power spectrum and  
the bispectrum provides much more accurate results  
than single probes

For details: Yankelevich&Porciani 2017, in prep.

New frontiers of cosmology  
is not far away

**Thank you  
for your attention**

